

$$\text{以上. } \int_{-1}^1 h(nx) \cdot \log(1+e^{x+1}) dx$$

$$= -\frac{1}{n} \int_{-1}^1 g(nx) \cdot f(x) dx \quad \text{かつ.}$$

$$f\left(-\frac{1}{n}\right) \leq n \int_{-1}^1 g(nx) \cdot f(x) dx \leq f\left(\frac{1}{n}\right) \quad \text{よ)}.$$

$$-f\left(\frac{1}{n}\right) \leq n^2 \int_{-1}^1 h(nx) \cdot \log(1+e^{x+1}) dx \leq -f\left(-\frac{1}{n}\right)$$

$$\lim_{n \rightarrow \infty} f\left(\frac{1}{n}\right) = \lim_{n \rightarrow \infty} f\left(-\frac{1}{n}\right) = f(0) = \frac{e}{1+e} \quad \text{よ)}.$$

ハサミの原理から

$$\lim_{n \rightarrow \infty} n^2 \int_{-1}^1 h(nx) \cdot \log(1+e^{x+1}) dx = -f(0) = -\frac{e}{1+e}$$